Graph Traversal Data Structures and Algorithms for Com (ISCL-BA-07) nal Linguistics III

Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de

Winter Semester 2020/21

Graph traversal

- atic way to visit all nodes in the graph · A graph trave Graph traversal is one of the basic tasks on a graph, answering many interesting questions
- Is there a path from one node to another?
 What is the shortest path (with minimum number of edges) between two
- - What is the shorter
 nodes?
 Is the graph conne
 Is the graph cyclic?

 - ain methods of traversals are breadth-first and depth-first

DFS - algorithm

- Wef dfs(start, visited-None):
 if visited is None:
 visited = fstart: None}
 for node in start.neighbors():
 if node not in visited:
 visited[node] = start
 dfs(node, visited)
- . Depth-first search (DFS) is easy with DFS starts from a start node · Marks each node it visits as visited (typically put it in a set data structure)
- Then, take an arbitrary unvisited neighbor and continue visiting the nodes recursively
- Algorithm terminates when backtracking leads to the start node with no unvisited nodes left

DFS - demonstration

 Depth first search follows the san idea as exploring a labyrinth with a string and a chalk

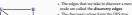
Visit each intersection (node), while marking the path you took

Mark each visited node, backtrack

(following the string) when hit a dead end

with the string

DFS - intuition



- · The discovery edges form the DFS tree · The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are
- The edges to a non-parent node in the DFS tree are called cross edges

DFS - demonstration



- . The edges that we take to discover a new
- node are called the discovery edges

 The discovery edges form the DFS tree * The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are called back edg
- . The edges to a non-parent node in the DPS tree are called

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges
 - . The discovery edges form the DFS tree · The other edges are called non-tree edges
 - . The edges to a parent in the DFS tree are
 - The edges to a non-parent node in the DFS tree are called cross edges

DFS - demonstration



- . The edges that we take to discover a new
- node are called the discovery edges * The discovery edges form the DFS tree
- * The other edges are called non-tree edges
- The edges to a parent in the DFS tree are called back edges
- * The edges to a non-parent node in the DPS tree are called cro

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges . The discovery edges form the DFS tree
- The other edges are called non-tree edges
- . The edges to a parent in the DPS tree are
- The edges to a non-parent node in the DFS tree are called cross edges.

DFS - demonstration



- . The edges that we take to discover a new
- node are called the discovery edges * The discovery edges form the DFS tree
- . The other edges are called non-tree edges
- The edges to a parent in the DFS tree are
- . The edges to a non-parent node in the DPS tree are called cros

DFS - demonstration



- The edges that we take to discover a new node are called the **discovery edges** The discovery edges form the DFS tree
- The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are
- The edges to a non-parent node in the DFS tree are called cross edges

- DFS demonstration



- The edges that we take to discover a new node are called the **discovery edges** The discovery edges form the DFS tree
- * The other edges are called non-tree edges * The edges to a parent in the DFS tree are
 - . The edges to a non-parent node in the DPS
 - tree are called cr

DFS - demonstration



- The edges that we take to discover a new node are called the **discovery edges** The discovery edges form the DFS tree
- The other edges are called non-tree edges . The edges to a parent in the DPS tree are

The edges to a non-parent node in the DFS tree are called cross edges.

DFS - demonstration

The edges that we take to discover a new node are called the discovery edges
 The discovery edges form the DFS tree

. The other edges are called non-tree edges

- * The edges to a parent in the DFS tree are
- . The edges to a non-parent node in the DPS tree are called cros

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges

 The discovery edges form the DFS tree
- · The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are
- . The edges to a non-parent node in the DFS tree are called cross

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges
- * The discovery edges form the DFS tree . The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are
- . The edges to a non-parent node in the DPS tree are called cros

DFS - demonstration



- . The edges that we take to discover a new
 - node are called the discovery edges
- · The discovery edges form the DFS tree · The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are
- called back ed The edges to a non-parent node in the DFS tree are called cross edges

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges
- . The discovery edges form the DFS tree . The other edges are called non-tree edges
- . The edges to a parent in the DFS tree are called back edges
- . The edges to a non-parent node in the DPS tree are called

DFS - demonstration



- . The edges that we take to discover a new node are called the discovery edges
 - . The discovery edges form the DFS tree · The other edges are called non-tree edges
 - . The edges to a parent in the DFS tree are
 - The edges to a non-parent node in the DFS tree are called cross edges

Properties of DFS

- . DFS visits all nodes in the co
- * Discovery edges form a spanning tree of the connected component If a node v is connected to the start node, there is a path from the start node v in the DFS tree
- The DFS algorithm visits each node and check each edge once (twice for
- undirected graphs) * The complexity of the algorithm is O(n+m) for n nodes and m edges

Dangers of DFS



BFS - intuition

- · A way to think about breadth-first search (BPS) is to explore all options
 - in parallel . In the maze, at every intersection
 - send out people in all directions

 BPS divides the nodes into levels:

 - starting node at level 0
 nodes directly accessible from start at level 1



BFS - algorithm

def bfs(start): lef bfs(start):
queue = [start]
visited = (start: None):
while queue:
current = queue.pop(o)
for mode in current.neighbors():
if mode not in visited:
 visited[node] = current
queue.append(node)

- · Typically implement BPS is implemented with a queue
- . If you replace the queue with a
- The algorithm visits nodes closest to the start node first stack, you get an iterative version of the DFS

BFS - demonstration



- * Similar to DFS, the edges that we take to discover a new node are called the discovery edges . The discovery edges form the BFS tree
- . The other edges are called non-tree edges
- . The edges to a parent in the BPS tree are called back edg
- . The edges to a non-parent node in the BFS tree are called cr

BFS - demonstration

- Similar to DFS, the edges that we take to discover a new node are called the **discov** edges
 - The discovery edges form the BFS tree
 - The edges to a parent in the BPS tree are

. The other edges are called non-tree edges

called back ed . The edges to a non-parent node in the BPS

tree are called co

- Similar to DFS, the edges that we take to discover a new node are called the discov
- edges . The discovery edges form the BFS tree
- . The other edges are called non-tree edges . The edges to a parent in the BFS tree are
- called back edg . The edges to a non-parent node in the BFS

tree are called co

BFS - demonstration



- . Similar to DFS, the edges that we take to discover a new node are called the discovery edges
 - The discovery edges form the BFS tree . The other edges are called non-tree edges
 - The edges to a parent in the BPS tree are called back ed
 - The edges to a non-parent node in the BFS tree are called cros

BPS - demonstration

BFS - demonstration



- Similar to DFS, the edges that we take to discover a new node are called the discovery edges The discovery edges form the BFS tree
- . The other edges are called non-tree edges . The edges to a parent in the BFS tree are called back edg
- The edges to a non-parent node in the BFS tree are called cro

BFS - demonstration



- . Similar to DFS, the edges that we take to discover a new node are called the discovery
- edges The discovery edges form the BFS tree
- . The other edges are called non-tree edges
- . The edges to a parent in the BFS tree are
- called back ed The edges to a non-parent node in the BFS tree are called cross edges.

Properties of BFS

- * DPS visits all nodes in the connected component from the start n
- * Discovery edges form a spanning tree of the connected component
 - = If a node ν is reachable from the start node, the BFS finds the shortest path from the start node to ν
 - . The BFS algorithm visits each node and check each edge * The complexity of the algorithm is O(n+m) for n nodes and m edges

Problems solved by graph traversals

- · Finding a path between two nodes (if one exists)
- Testing whether G is connected
- Computing connected components of G
- Detecting cycles

Finding a path between two nodes

- Traverse the graph from the source node, record the discovery edges
- . Start from the target node. trace the path back to the source

Summary

- With BPS, we get the shortest path
- def find path(source, target, visited):
 path = []
 if target in visited:
 path.append(target)
 current = target
 - while current is not source parent = visited[current] path.append(parent) current = parent return path.reverse()

* Running time is the length of the path: O(n)

Some other problems solved by graph traversal

- · Is the graph connected?
- Yes if the 'visited' nodes have the same length as the nodes of the graph · Find the connected components Run traversal multiple times, until all nodes are visit
- · Is the graph cyclic? A graph is cyclic if there is a back edge during graph traversal

- · Traversal is one of the basic operations in graphs Graph traversals already solve some interesting prob
 Find a path (shortest with BFS)
 Tost connectivity, find connected components Find cycles
- Reading on graphs: goodrich2013
- More graph algorithms: special problems on directed graphs, shortest paths

Acknowledgments, credits, references

