

## Finite state transducers

Data Structures and Algorithms for Computational Linguistics III  
(ISCL-BA-07)

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## Finite state transducers

A quick introduction

- A *finite state transducer* (FST) is a finite state machine where transitions are conditioned on pairs of symbols
- The machine moves between the states based on an *input* symbol, while it outputs the corresponding *output* symbol
- An FST encodes a *relation*, a mapping from a set to another
- The relation defined by an FST is called a *regular* (or *rational*) relation



## Formal definition

Introduction Operations on FSTs Determinizing FSTs Summary

A finite state transducer is a tuple  $(\Sigma_i, \Sigma_o, Q, q_0, F, \Delta)$   
 $\Sigma_i$  is the *input* alphabet  
 $\Sigma_o$  is the *output* alphabet  
 $Q$  a finite set of states  
 $q_0$  is the start state,  $q_0 \in Q$   
 $F$  is the set of accepting states,  $F \subseteq Q$   
 $\Delta$  is a relation  $(\Delta : Q \times \Sigma_i \rightarrow Q \times \Sigma_o)$

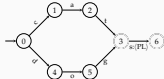
## Where do we use FSTs?

Uses in NLP/CL

- Morphological analysis
- Spelling correction
- Transliteration
- Speech recognition
- Grapheme-to-phoneme mapping
- Normalization
- Tokenization
- POS tagging (not typical, but done)
- partial parsing / chunking
- ...

## Where do we use FSTs?

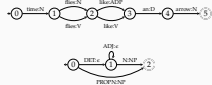
example 1: morphological analysis



In this lecture, we treat an FSA as a simple FST that outputs its input: the edge label 'a' is a shorthand for 'aa'.

## Where do we use FSTs?

example 2: POS tagging / shallow parsing



Note: (1) It is important to express the ambiguity. (2) This gets interesting if we can 'compose' these automata.

## Closure properties of FSTs

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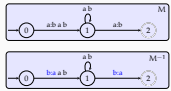
Like FSA, FSTs are closed under some operations.

- Concatenation
- Kleene star
- Complement
- Reversal
- Union
- Intersection
- Inversion
- Composition

## FST inversion

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- Since an FST encodes a relation, it can be reversed
- Inverse of an FST swaps the input symbols with output symbols
- We indicate inverse of an FST  $M$  with  $M^{-1}$



## FST composition

sequential application

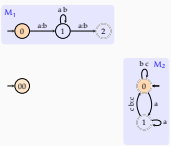


aa	$M_{1+}$	$M_{2+}$	bb
bb	$M_{1+}$	$\emptyset$	$M_{2+}$
aaaa	$M_{1+}$	$M_{2+}$	baac
abaa	$M_{1+}$	$M_{2+}$	bbac

Can we compose two FSTs without running them sequentially?

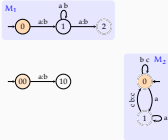
## FST composition

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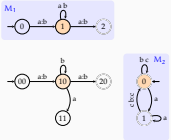
## FST composition

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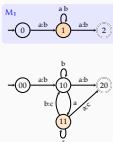


## FST composition

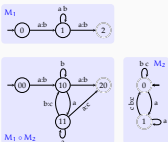
Introduction Operations on FSTs Determinizing FSTs Summary



## FST composition



## FST composition



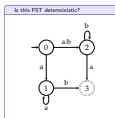
## Projection

- Projection turns an FST into a FSA, accepting either the input language or the output language



## FST determinization

- A Deterministic FST has unambiguous transitions from every state on any input symbol
- We can extend the subset construction to FSTs
- Determinization of FSTs means converting to a subsequential FST
- However, not all FSTs can be determinized



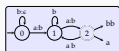
## Sequential FSTs

- A sequential FST has a single transition from each state on every input symbol
- Output symbols can be strings, as well as  $c$
- The recognition is linear in the length of input
- However, sequential FSTs do not allow ambiguity



## Subsequential FSTs

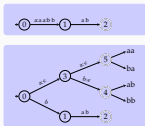
- A  $k$ -subsequential FST is a sequential FST which can output up to  $k$  strings at an accepting state
- Subsequential transducers allow limited ambiguity
- Recognition time is still linear



- The 2-subsequential FST above maps every string it accepts to two strings, e.g.,
  - $- \text{baa} \rightarrow \text{bbba}$
  - $- \text{baa} \rightarrow \text{bbbb}$

## An exercise

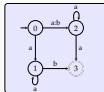
Convert the following FST to a subsequential FST



## Determinizing FSTs

Another example

Can you convert the following FST to a subsequential FST?



Note that we cannot 'determine' the output on first input, until reaching the final input.

## FSA vs FST

- FSA are acceptors, FSTs are transducers
- FSA accept or reject their input, FSTs produce output(s) for the inputs they accept
- FSA define sets, FSTs define relations between sets
- FSTs share many properties of FSAs. However,
  - FSTs are not closed under intersection and complement
  - We can compose (and invert) the FSTs
  - Determinizing FSTs is not always possible
- Both FSA and FSTs can be weighted (not covered in this course)

## References / additional reading material

- Jurafsky and Martin (2009, Ch. 3)
- Additional references include:
  - Roche and Schabes (1996) and Roche and Schabes (1997): FSTs and their use in NLP
  - Mohri (2009): weighted FSTs

## References / additional reading material (cont.)

- Jurafsky, Daniel and James H. Martin (2009). *Speech and Language Processing: An Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition*, second edition. Pearson Prentice Hall. isbn: 978-0-13-504196-3.
- Mohri, Mehryar (2009). "Weighted automata algorithms". In: *Handbook of Weighted Automata*. Monographs in Theoretical Computer Science. Springer, pp. 213–254.
- Roche, Emmanuel and Yves Schabes (1996). *Introduction to Finite-State Devices in Natural Language Processing Technical Report*. Tech. rep. TR96-13. Mitsubishi Electric Research Laboratories. URL: <http://www.merl.com/publications/docs/TR96-13.pdf>.
- (1997). *Finite-state Language Processing*. A Bradford book. MIT Press. isbn: 9780262181822.

