Minimization of FSA

Data Structures and Algorithms for Comp (ISCL-BA-07) nal Linguistics III

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Winter Semester 2020/21



The edges leaving the group of nodes are identical. Their right languages are the same

Minimization by partitioning

Finding equivalent states



- Accepting & non-accep partition
- If any two nodes go to different sets for any of the symbols split
- $\bullet \ \ Q_1=\{0,3\}, Q_2=\{1\}, Q_3=\{2\}, Q_2=\{4,5\}$
- Stop when we cannot split any of the sets, merge the indistinguishable states

DFA minimization

- · For any regular language, there is a unique minimal DFA By finding the minimal DFA, we can also prove equivalence (or not) of different FSA and the languages they recognize
- · In general the idea is:
- in goatest acte acted to consider states (easy)
 Merge equivalent states
 There are two well-known algorithms for minimization:
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 Hopcord's algorithms find and eliminate equivalent states by partitioning the set of states
 Bizzazowski's algorithms: (double reversal)

Finding equivalent states



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Minimization by partitioning



* Create a state-by-state table, mark distinguishable pairs: (q_1,q_2) such that $(\Delta(q_1,x),\Delta(q_2,x))$ is a distinguishable pair for any $x\in\Sigma$



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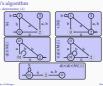


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- The algorithm can cell to visit carefully

Brzozowski's algorithm



An exercise





Minimization algorithms

- There are many versions of the 'partitioning' algorithm. Gene form equivalence classes based on right-language of each state.
- Partitioning algorithm has O(n log n) complexity · 'Double reversal' algorithm has exponential worst-time complexity
- Double reversal algorithm can also be used with NFAs (resulting in the minimal equivalent DFA NFA minimization is intractable) In practice, there is no clear winner, different algorithms run faster on
- rent input Reading suggestion: Martin (2009, Ch. 2) : Hopcroft and Ullman (1979, Ch. 2&3), Jurafsky and
- PSA determinization, minimization

Acknowledgments, credits, references

Hopcroft, John E. and Jeffrey D. Ullman (1979). Introduction to Automata Theory, Languages, and Computation. Addison-Wesley Series in Computer Science and

Languages, and Computation. Addison-Wesley Series in Computer Science and Information Processing. Addison-Wesley. user 9902011205889. Jurafsky, Daniel and James H. Martin (2009). Speech and Language Processing: As Introduction to Natural Language Processing, Computational Linguistics, and Speech Recognition. second edition. Pearson Prentice Hall. user: 978-013-304198-3.

