NFA determinization Data Structures and Algorithms for Computa (ISCL-BA-07) tional Linguistics III Çağrı Çöltekin ccoltekin@sfs.uni-tuebingen.de

Winter Semester 2020/21

NFA recognition (again)

Input: a b a b

NFA recognition (again)

- 1. Start at a 2. Take the next input, mark all possible next
 - 3. If an accepting state is marked at the end of
 - the input, accept

Take the next input, mark all possible next

1. Start at qo

3. If an accepting s the input, accept Recap

white stake automata course in www.awvo.s

— Deterministic (DFA): linear recognition time

— Deterministic (NFA): sometimes more intuitive, easy to define, but expo

The DFA and NFA are equivalent: for any language recognized by an NFA

there is also a DFA recognizing the same language . Then, the question is: how can we determinize an NFA to obtain an equivalent

NFA recognition (again)

- 1. Start at q 2. Take the next input, mark all possible next
 - If an accepting state is marked at the end of the input, accept

Input a b a b



tabab

- 1. Start at q
- Take the next input, mark all possible next
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NFA recognition (again)

1. Start at go 2. Take the next input, mark all possible next

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NFA recognition (again)



Input a b a b

1. Start at go 2. Take the next input, mark all possible next

- If an accepting state is marked at the end of the input, accept

The process is deterministic, and finite-state

Determinization

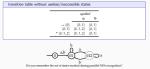
Intuition: remember the parallel NFA recognition. We can consider an NFA being a deterministic machine which is at a set of states at any given time.

- Subset construction (sometimes called power set construction) uses th intuition to convert an NFA to a DFA The algorithm can be modified to handle c-transitions (or we can elimit

c's as a preprocessing step)

The subset construction

transition table without useless/inaccessible sta



transition table with subsets a {0,1} {0,1} (0, 2) (0) (0, 1, 2) (0, 1) {0, 1} (0,1,2) (0,1) * {1,2} (0,1,2) * {0,1,2} {0,1,2} 60 13

The subset construction

NEA



· What language do they recognize?

Yet another exercise The subset construction In worst case, resulting DFA has 2ⁿ nodes Determinize the following automaton Worst case is rather rare, number of nodes in an NFA and the converted DFA - In practice, we do not need to enumerate all 2^n subsets We've already seen a typical problematic case: ab ab ab ab ab ab 4 Summary Acknowledgments, credits, references · PSA are efficient tools with many applications * PSA have two flavors: DEA, NEA (or maybe three: ε-NEA) B. Hopeneth, John E. and Jeffrey D. Ullmans (1899). Introduction to Automate Theory, Languages, and Computation. Addison Worley Service to Compute Science and Information Processing, Addison-Worley-ruse 970020102998.

Juraficky, Daniel and James H. Martin (2009). Speech and Language Processing, Can Introduction to Natural Language Processing. Computational Linguistics, and Speech Introduction to Natural Language Processing. Computational Linguistics, and Speech Recognitions, second edition. Pleasant Prefix I feld. Introduction to Vision II Supress of Profits (1997). · DFA recognition is linear, recognition with NFA may require Reading suggestion: Hopcroft and Ullman (1979, Ch. 2&3), Jurafsky and Martin (2009, Ch. 2) Minimizatie